ECE THEORY OF THE LAMB SHIFT IN ATOMIC HYDROGEN AND HELIUM

by

Myron W. Evans,

Civil List Scientist

(<u>www.aias.us</u> and <u>emyrone@aol.com</u>)

and

Horst Eckardt,

A.I.A.S Fellow

(horsteck@aol.com)

ABSTRACT

The ECE theory of the Lamb shift in atomic hydrogen and helium is developed using considerations of the centrifugal repulsion in atomic hydrogen and the Coulomb and exchange integrals in atomic helium. Radiative corrections are applied using the same method as for the anomalous g factor of the electron and as developed in previous work for atomic hydrogen without the centrifugal correction. The results are expressed systematically in terms of a parameter r(vac) that measures the effect of radiative correction on the radial and other orbitals. This method can be extended systematically in quantum chemistry packages, which can be used for example to numerically generate radial orbitals for use with this method. The latter may have important consequences in obtaining new sources of energy from space-time, (i.e. the source of radiative corrections).

Keywords: Einstein Cartan Evans (ECE) theory, Lamb shift in atomic hydrogen and helium, energy from space-time.

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1. INTRODUCTION

Recently {1} the Einstein Cartan Evans unified field theory {2-12} has been applied to the determination of the Lamb shift in atomic hydrogen using a method that succeeded in reproducing the g factor of the electron to experimental uncertainty. The results of the calculation were expressed in terms of a radial parameter r(vac) which demonstrates the way in which the radiative correction affects each orbital. The Lamb shift in atomic H {13} was produced satisfactorily using this method, which has no free parameters. In this paper the method is extended to atomic hydrogen with consideration of centrifugal repulsion {14} as well as Coulombic attraction, and to atomic helium, which consists of two electrons and two protons. The results are again in satisfactory agreement with data, and can be extended systematically using quantum chemistry packages such as density functional code. The overall aim is to find methods of amplifying the radiative correction by resonance, so that free electrons are released and used for power generation in circuits.

In Section 2 the method is used for the complete potential of atomic hydrogen, which is well known {14} to contain a centrifugal repulsion term as well as the Coulomb attraction between electron and proton. The result is expressed in terms of r(vac) and graphical data produced for the relevant orbitals. The original Lamb shift {15} was discovered between the 2s and 2p orbitals of hydrogen, and this method naturally removes the angular dependence, so that only radial orbitals need be considered {14}.

In Section 3 the method is extended to atomic helium, and considerations given to the Coulomb and exchange integrals {14} in order to understand the basic features of multi electron atoms. If a method is found to resonate r(vac) to infinity, the atom will dissociate into free electrons which can be used for powering circuits. The source of this power is spacetime, which is also the source of the radiative correction in ECE theory. Therefore the methods of this paper complement previous considerations {2-12} of ionization of atoms

using spin connection resonance {16}.

2. ATOMIC HYDROGEN WITH CENTRIFUGAL EFFECTS

In this paper the non-relativistic quantum limit of the ECE wave equation {2-12} is ... used, the Schrodinger equation considered in a causal and objective interpretation of quantum mechanics rather than the Copenhagen interpretation. The Schrodinger equation of atomic hydrogen {14} is:

$$-\frac{2}{2m}\nabla^{3}\psi - \frac{e^{3}}{4\pi\epsilon \cdot r}\psi = E\psi - (1)$$

where **n** is the reduced mass, h is the reduced Planck constant, **c** Is the S.I. vacuum permittivity, e is the charge on the proton, -e is the charge on the electron, r is the radial distance between electron and proton, E is the total energy and **v** is the wave-function. By expressing the laplacian in spherical polar coordinates, the equation of the spherical harmonics is introduced:

$$\nabla \lambda = -6(6+1)\lambda - (3)$$

where $Y(\theta, \phi)$ are the spherical harmonics {14} and l is the angular momentum quantum number. The solution of Eq. (Δ) is:

$$\psi(i,\theta,\phi) = R(i)Y(\theta,\phi) - {3 \choose 3}$$

$$-\frac{2}{3m}\frac{d^{2}P}{dt^{2}}-V_{eff}^{(0)}P=EP-(4)$$

where the effective potential is:

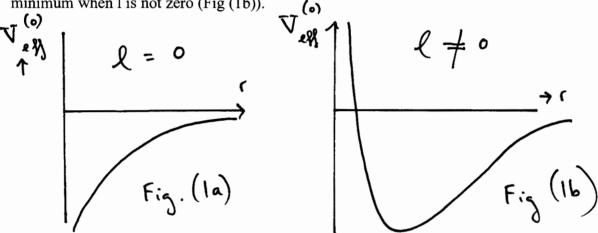
$$\nabla_{ell}^{(0)} = -\frac{e^{2}}{4\pi\epsilon_{0}r} + \ell(\ell+1)\frac{1}{2\pi r^{2}} - (5)$$

and where:

$$P = rR \qquad \qquad - \left(6 \right)$$

The second term in eq. (5) is the centrifugal repulsion and the complete potential has a

minimum when l is not zero (Fig (1b)).



The radiative correction that leads to the Lamb shift {1} is now incorporated by

changing Eq. (4) to:

$$-\frac{R^{2}}{2m}\left(1+\frac{d}{dr}\right)^{2}\frac{d^{2}P}{dr^{2}}-V_{eff}^{(0)}P=EP-(7)$$

where χ is the fine structure constant. This equation is equivalent by hypothesis $\{1\}$ to:

$$-\frac{R^2}{2\pi}\frac{d^2P}{dx^2}-V_{eff}P=EP-(8)$$

where:

$$V_{eff} = \frac{e^{3}}{4\pi \epsilon \cdot (1+i(vac))} - \frac{\ell(\ell+1)t^{3}}{2m(1+i(vac))^{3}} - \frac{(a)}{2m(1+i(vac))^{3}}$$

Here $r(\sqrt{46c})$ is the extent to which the radiative correction perturbs the electron in each orbital.

To first order in
$$d$$
:
$$-\frac{2^{2}d}{4\pi^{2}} \frac{d^{2}p}{dt^{2}} = \left(\sqrt{\frac{6}{4}}\right) - \sqrt{\frac{10}{4}}$$

where

to a very good approximation, because the Lamb shift in hydrogen is very small compared with the total energy of the unperturbed orbitals. Therefore:

$$\nabla = \frac{e^2}{4\pi \epsilon} \left(\frac{1}{r} - \frac{1}{1+r(vac)} \right) - \frac{\ell(\ell+1)t^2}{2m} \left(\frac{1}{r^2} - \frac{1}{(r+r(vac))^2} \right)$$

and Eq. (10) is solved for r(vac) for each orbital, the result being different for each orbital. Specifically there is a difference between the 2s and 2p orbitals, giving the Lamb shift. The experimental value of the latter is used to find r(vac). Computer algebra is used to solve Eq. (10) and the results are graphed in Section 4.

3. ATOMIC HELIUM

This atom consists of two electrons and two protons and its Schrodinger equation

is:
$$H_{+} = \frac{P^{2}}{2m} \left(\sqrt{3} + \sqrt{3} \right) - \frac{2e^{2}}{4\pi f_{0} f_{1}} - \frac{2e^{2}}{4\pi f_{0} f_{3}} + \frac{e^{2}}{4\pi f_{0} f_{3}} - \frac{14}{4\pi f_{0} f_{3}} \right)$$

$$- \left(\frac{14}{4\pi f_{0}} \right)$$

where \underline{r} is the distance between electron 1 and the nucleus and similarly for \underline{r} . The Coulombic terms are doubled because there are two protons giving twice the attractive force. There is also an electron electron repulsion, where r is the distance between the two electrons. The inter-electron term can be expanded in terms of spherical harmonics:

$$\frac{1}{\zeta_{13}} = \frac{1}{\zeta_{1}} \sum_{\ell=0}^{\infty} \sum_{m_{e}=1}^{\ell} \left(\frac{|\psi_{1}|}{2\ell+1} \right) \left(\frac{\zeta_{2}}{\zeta_{1}} \right)^{\ell} \sum_{\ell m_{e}} \left(\theta_{1}, \phi_{1} \right) \sum_{\ell m_{e}} \left(\theta_{2}, \phi_{2} \right) - (15)$$

if $r > r_2$, and inter-change r_3 and r_3 when $r_3 > r_3$. This gives rise {14} to the Coulomb integral:

For example, if we consider the interaction energy between two electrons in a hydorgen liek 1s orbital {14}, then:

$$\varphi\left(\Sigma_{1}\right)=\left(\frac{7^{3}}{\pi a_{0}^{3}}\right)^{1/2}\exp\left(-\frac{7}{a_{0}}\right)-\left(17\right)$$

$$\psi(z) = \left(\frac{2^{3}}{\pi a_{0}^{3}}\right)^{1/3} exp\left(-\frac{2}{a_{0}}\right) - (18)$$

and it is found that:

$$\frac{1}{\frac{1}{2}} = \frac{1}{\frac{1}{2}}, \frac{2}{2}, \frac{2}{2}, \frac{1}{2}$$

These results can be used to calculate J analytically:

$$J = \frac{5}{8} \frac{e^{2}}{4\pi f_{0}} \frac{7}{a_{0}} - (20)$$

It is found that {14}:

$$\mathcal{I} = \frac{2}{16} \left(3E^{12} \right) - \left(31 \right)$$

so the electron electron repulsion is a substantial fraction of the unperturbed total energy of the 1s orbital in helium. The aim of this section is to incorporate radiative corrections into the helium atom, which also contains the well known exchange integral leading to Fermi heap and hole theory {14}.

The Schrödinger equation of atomic helium is:

where:

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It is assumed that there is an unperturbed hamiltonian {14} which is the sum of two hydrogen like hamiltonians:

where:

The factor two in the numerator of the second term comes from the fact that there are two electrons and two protons, so each electron is attracted by two protons. The assumption () means that the total wave-function must be the product {14}:

The total unperturbed energy levels are {14}

$$E = -4 \operatorname{Rc}_{\phi} \left(\frac{1}{n_1^2} + \frac{1}{n_2^2} \right) - (37)$$

where R is the Rydberg constant.

To incorporate radiative corrections the first step is to develop Eq. (35) and write it as:

$$H: -\frac{2^{2}}{2m} \frac{d^{2}}{dx_{i}^{2}} - V_{eff}^{(0)}, \quad -(28)$$

where

$$V_{ell,i}^{(0)} = -\frac{e^{2}}{2\pi f_{0}r_{i}} + \frac{\ell(\ell+1)t^{2}}{mr_{i}^{2}} - (29)$$

So there are two hydrogen like equations:

are two hydrogen like equations:
$$-\frac{1}{2m}\frac{1^{2}P}{4K_{1}^{2}}-V_{\text{ell},1}^{(0)}P=E_{1}P-(30)$$

$$-\frac{1}{2m}\frac{1^{2}P}{4K_{2}^{2}}-V_{\text{ell},2}^{(0)}P=E_{2}P-(31)$$

where:

$$\nabla_{e0,1}^{(i)} = -\frac{e^{3}}{2\pi f_{i} f_{i}} + \frac{\ell(\ell+1)\ell^{3}}{m f_{i}^{3}} - \binom{33}{33}$$

$$\nabla_{e0,2}^{(i)} = -\frac{e^{3}}{2\pi f_{i} f_{i}} + \frac{\ell(\ell+1)\ell^{3}}{m f_{i}^{3}} - \binom{33}{33}$$

Radiative corrections are incorporated into Eqs. (30) to (31) as in Eqs. (8) to). For each r and r there will be a corresponding r (vac) and r (vac) and the total wave-function is the product as in Eq. (26). These radiative corrections may then be incorporated sytematically into the Coulomb and exchange integrals using the expansion (15) of r in terms of r and r . With radiative corrections:

By hypothesis, Eqs. () and (31) become:

is, Eqs. (30) and (31) become:

$$-\frac{2^{3}}{2^{m}}\frac{d^{3}p}{dx_{1}^{3}} - \nabla_{ey}, \quad P = E_{1}p - (36)$$

$$-\frac{2^{3}}{2^{m}}\frac{d^{3}p}{dx_{2}^{3}} - \nabla_{ey}, \quad P = E_{3}p - (37)$$

with:

$$\frac{d^{2}}{dx_{1}^{2}} \rightarrow \begin{pmatrix} 1+\frac{d}{dx} \end{pmatrix}^{2} \frac{d^{2}}{dx_{1}^{2}} - \begin{pmatrix} 38 \end{pmatrix}$$

$$\frac{d^{2}}{dx_{2}^{2}} \rightarrow \begin{pmatrix} 1+\frac{d}{dx} \end{pmatrix}^{2} \frac{d^{2}}{dx_{2}^{2}} - \begin{pmatrix} 38 \end{pmatrix}$$
where:
$$V_{AB,1} = \frac{e^{2}}{2\pi \ell_{0} \left(r_{1} + r_{1} \left(v_{0} c_{1} \right) \right)} - \frac{\ell \left(\ell+1 \right) \ell^{2}}{\left(r_{1} + r_{1} \left(v_{0} c_{1} \right) \right)^{2}} - \begin{pmatrix} l_{+1} \end{pmatrix}$$

$$V_{AB,1} = \frac{e^{2}}{2\pi \ell_{0} \left(r_{1} + r_{2} \left(v_{0} c_{1} \right) \right)} - \frac{\ell \left(\ell+1 \right) \ell^{2}}{\left(r_{2} + r_{2} \left(v_{0} c_{1} \right) \right)^{2}} - \begin{pmatrix} l_{+1} \end{pmatrix}$$
To first order in $d: = \begin{pmatrix} l_{+1} \end{pmatrix} \begin{pmatrix} l_{+$

and this may be evaluated with computer algebra with radiative corrections. Finally a search may be made numerically for conditions under which r(vac) becomes very large. Under such conditions the atom may ionize, giving free electrons. This idea complements previous work {2-12} using spin connection resonance {17}. The overall method can be systematically extended by using quantum chemistry software to generate radial wave-functions with which radiative corrections can be considered.

Table 1				
F	iist f	Five	Orsital	5 of Atomic H
	h	1	me	d nene $(1,0,4)$
\s	l	0	٥	$exp\left(-\frac{c}{a}\right)$
٦s	٦	0	٥	$\left(2-\frac{r}{a}\right)$ $exp\left(-\frac{r}{2a}\right)$
765	ک	١	٥	$\frac{1}{\alpha} \cos \theta \approx \sqrt{-\frac{1}{2\alpha}}$
~) \	2	١	l	$-\frac{\Gamma}{a} Sih \theta \exp\left(i\phi\right) \exp\left(-\frac{\Gamma}{2a}\right)$
264	2	1	-1	$\frac{\Gamma}{a} \sin \theta \exp(-i\phi) \exp(-\frac{\Gamma}{2a})$
	·			