

# 392(6): Final Veria of Scheme of Computation and Order of Calculation

1) Find  $\phi$  and  $\underline{A}$  from the ECE wave equations:

$$\nabla^2 \phi = \rho / \epsilon_0 \quad - (1)$$

$$\nabla^2 \underline{A} = \mu_0 \underline{J} \quad - (2)$$

The general solutions for  $\phi$  and  $\underline{A}$  are the Lienard-Wiechert potentials. For considerations of the anomalies of the electron, let  $\rho$  and  $\underline{J}$  contain vacuum contributions. So, let  $\phi$  and  $\underline{A}$  contain vacuum contributions. The charge density  $\rho$  and current density  $\underline{J}$  are related by the continuity equation:

$$\frac{\partial \rho}{\partial t} + \nabla \cdot \underline{J} = 0 \quad - (3)$$

2) Consider the homogeneous field equations:

$$\nabla \cdot \underline{B} = 0 \quad - (4)$$

$$\nabla \times \underline{E} + \frac{\partial \underline{B}}{\partial t} = \underline{0} \quad - (5)$$

These are solved automatically by defining:

$$\underline{E} = -\nabla \phi + \underline{\omega} \phi = -\nabla \phi - \frac{\partial \underline{A}(\text{total})}{\partial t} \quad - (6)$$

and

$$\underline{B} = \nabla \times \underline{A} - \underline{\omega} \times \underline{A} = \nabla \times (\underline{A} + \underline{A}_1)$$

$$= \nabla \times \underline{A}(\text{total}) \quad - (7)$$

So:

$$-\frac{\partial \underline{A}_1}{\partial t} := \underline{\omega} \phi \quad - (8)$$

$$\nabla \times \underline{A}_1 := -\underline{\omega} \times \underline{A} \quad - (9)$$

Therefore  $A_1$  is the shadow or longitudinal potential that defines the interaction with the vacuum.

Find  $\underline{\omega}$  from  $\underline{A}$  using vector calculus:

$$\frac{\partial A_z}{\partial y} + \frac{\partial A_y}{\partial z} = \omega_y A_z + \omega_z A_y \quad - (10)$$

$$\frac{\partial A_x}{\partial z} + \frac{\partial A_z}{\partial x} = \omega_z A_x + \omega_x A_z \quad - (11)$$

$$\frac{\partial A_y}{\partial x} + \frac{\partial A_x}{\partial y} = \omega_x A_y + \omega_y A_x \quad - (12)$$

where  $\underline{A}$  is the Liénard-Wiechert vector potential defined by eq. (2)

Find: 
$$\frac{1}{c^2} \frac{\partial^2 \phi}{\partial t^2} = \nabla \cdot (\underline{\omega} \phi) \quad - (13)$$

where  $\phi$  is the Liénard-Wiechert scalar potential from eq. (1), and where  $\underline{\omega}$  is found from eqs. (10) to (12).

Find  $\nabla^2 \phi$  from eqs. (1) and (13):

$$\frac{1}{c^2} \frac{\partial^2 \phi}{\partial t^2} - \nabla^2 \phi = \frac{\rho}{\epsilon_0} \quad - (14)$$

The charge density  $\rho$  is measured in a material or circuit and always contains contributions from the vacuum.

b) From eq. (13), find:

$$3) \frac{1}{c^2} \frac{\partial \phi}{\partial t} = \int \underline{\nabla} \cdot (\underline{\omega} \phi) dt - (15)$$

7) Find  $\omega_0$  from tree antisymmetry conservation:

$$\frac{1}{c^2} \left( \frac{\partial}{\partial t} + \omega_0 \right) \phi = (\underline{\nabla} - \underline{\omega}) \cdot \underline{A} - (16)$$

8) Find  $-\partial \underline{A} / \partial t$  from scalar antisymmetry conservation:

$$\underline{E} = -\underline{\nabla} \phi + \underline{\omega} \phi = -\frac{\partial \underline{A}}{\partial t} - \omega_0 \underline{A} - (17)$$

9) Find  $\partial^2 \underline{A} / \partial t^2$  from  $\partial \underline{A} / \partial t$  and find  $\nabla^2 \underline{A}$

$$\text{from: } \frac{1}{c^2} \frac{\partial^2 \underline{A}}{\partial t^2} - \nabla^2 \underline{A} = \mu_0 \underline{J} - (18)$$

$$10) \text{ Compute: } \underline{E} = -\underline{\nabla} \phi + \underline{\omega} \phi = -\frac{\partial \underline{A}}{\partial t} - \omega_0 \underline{A} - (19)$$

11) Compute the shadow fields:

$$\underline{E}_1 = \underline{\omega} \phi - (20)$$

$$\text{and } \underline{E}_2 = -\omega_0 \underline{A} - (21)$$

These are maps of the vacuum.

$$12) \text{ Compute: } \underline{B} = \underline{\nabla} \times \underline{A} - \underline{\omega} \times \underline{A} - (22)$$

and the shadow magnetic field:

$$\underline{B}_1 = -\underline{\omega} \times \underline{A} \quad (23)$$

this is another way of Q vacuum.

4) couple Q standard model fields:

$$\underline{E}_s = -\underline{\nabla} \phi - \frac{\partial \underline{A}}{\partial t} \quad (24)$$

$$\underline{B}_s = \underline{\nabla} \times \underline{A} \quad (25)$$

in order to provide a comparison with eqs. (6) and (7).

### Discussion

This is a standard scheme of computation for electrodynamics. It gives a completely self consistent scheme of computation while avoiding iterative computation. It can also be used for electrostatics and magnetostatics, and for gravitation and fluid dynamics.