

224(5): Reputation of the  $U(1)$  Sector w/ Antisymmetry.

In  $U(1)$  electrodynamics of the standard model the field tensor is defined by:

$$F_{\mu\nu} = \partial_\mu A_\nu - \partial_\nu A_\mu. \quad - (1)$$

By antisymmetry (antisymmetry of the field tensor):

$$\partial_\mu A_\nu = -\partial_\nu A_\mu \quad - (2)$$

and in vector notation:

$$\underline{\nabla} \phi = \frac{\partial \underline{A}}{\partial t}, \quad - (3)$$

$$\frac{\partial A_j}{\partial x_i} = -\frac{\partial A_i}{\partial x_j} \quad - (4)$$

This implies that:

$$\underline{\nabla} \times \frac{\partial \underline{A}}{\partial t} = \underline{\nabla} \times \underline{\nabla} \phi = 0 \quad - (5)$$
$$= \frac{\partial}{\partial t} (\underline{\nabla} \times \underline{A})$$

In the standard model:

$$\underline{E} = -\underline{\nabla} \phi - \frac{\partial \underline{A}}{\partial t}, \quad - (6)$$

$$\underline{B} = \underline{\nabla} \times \underline{A} \quad - (7)$$

From eqs. (5) and (7):

$$\frac{\partial \underline{B}}{\partial t} = \underline{0} \quad - (8)$$

The Faraday law of induction is the

2) standard model is:

$$\underline{\nabla} \times \underline{E} + \frac{\partial \underline{B}}{\partial t} = \underline{0} \quad - (9)$$

so

$$\underline{\nabla} \times \underline{E} = \underline{0} \quad - (10)$$

Therefore  $\underline{B}$  is a static magnetic field, so

$\underline{E}$  is also a static ~~magnetic~~ electric field.

If  $\underline{B}$  is static, then:

$$\frac{\partial \underline{A}}{\partial t} = \underline{\nabla} \phi = \underline{0} \quad - (11)$$

and so:

$$\underline{E} = ? \underline{0} \quad - (12)$$

Antisymmetry leads to the collapse of the  $u(1)$  vector symmetry because the electric field disappears and the magnetic field is static.

Therefore the entire theory of the Higgs boson collapses. It is said to be a  $u(1)$  vector symmetry.