

161(3):

This is: $T = \hbar \omega = (\gamma - 1) mc^2 \quad - (1)$

for all particles.

Energy Conservation

This leads to the same result:

$$m_2 = \frac{\hbar}{c^2} (\omega'' + \omega' - \omega) \quad - (2)$$

Momentum Conservation

It leads to:

$$\begin{aligned} \frac{1}{\omega''} (\omega''^2 - x_2^2) (\omega''^2 + x_2^2) &= \frac{1}{\omega^2} (\omega^2 - x_1^2) (\omega^2 + x_1^2) + \frac{1}{\omega'^2} (\omega'^2 - x_1^2) (\omega'^2 + x_1^2) \\ &\quad - \frac{2}{\omega \omega'} (\omega^2 - x_1^2)^{1/2} (\omega'^2 - x_1^2)^{1/2} (\omega + x_1) (\omega' + x_1) \cos \theta \end{aligned} \quad - (3)$$

and eq. (2).

Eqs. (2) and (3) can be solved in principle, but are very complicated.
